

## Discussion: Modelling baseline excess hazard function in relative survival

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### Statement of Interest!

- I am biased!
- Nelson's approach is essentially that of Royston & Parmar (2002)
- 5 years later, I still like the approach
- I therefore encourage Nelson and others to research this family of models further

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### Bernard Rachet

- Time and covariates are not (or need not be) categorised
- FPs and/or regression splines as functions of time for modelling baseline excess hazard
- ... also for interactions of covariates with time
- Principled approach to model selection using MFP

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### Issues with Rachet's approach

- Modelling the excess hazard with FPs/splines may give artefacts in the curves
- "How flexible?" seems to be a general issue
  - Particularly with large datasets
  - Criteria for model selection?
- Selecting interaction models – may be too flexible, leading to instability/possible interpretation problems
  - Breast cancer example
- May need expert "tuning" to get good results

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### Chris Nelson

- Main difference: modelling *cumulative* excess hazard function
- Splines in log t for this function
- Can also model covariates in similar fashion

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### Some issues with categorisation (Nelson)

- Several methods split the timescale into manageable chunks for estimation purposes
  - Necessary with large datasets
- Collapse on time and grouped covariates
  - Can't handle continuous covariates
- Piecewise models could be considered as biologically implausible, both for time and covariates (also, biased?)

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- Many parameters for time-dependent effects
  - Time chunks x covariate groups = lots
  - Overfitted, unrealistic
  - Can lead to problems in smaller datasets, e.g. zero cells
- If have many observations, may get computation-time problems on split data
- Methods that do *not* split time require integration to estimate survival function
  - Because estimating excess hazard, not cumulative

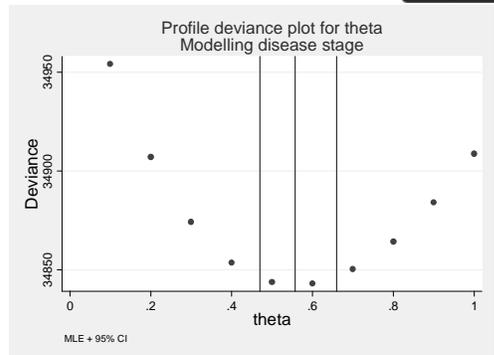
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**Comments**

- For me, Nelson’s approach is close to the method of choice
- Could substitute fractional polynomials for splines in some applications (Lambert, Rachtel)
  - Model baseline cumulative excess hazard
  - Model continuous covariates
- Don’t forget the other link functions
  - $\Theta = 1$  (cumulative proportional odds)
  - $\Theta \neq 0, 1$  (can be estimated from the data)

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**Colon cancer data – stage known**



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**Regression splines – in favour**

- Parametric
  - Concise description of function available
- Flexible
  - Can cope with many different curve shapes
- Can control flexibility via number of knots
  - Not usually too sensitive to exact knot positioning
- Easily incorporated in regression models
  - No special computational methods required

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**Regression splines – against**

- Baseline cumulative excess hazard function not guaranteed monotonic in time
- Model (knot) selection – is AIC satisfactory?
  - No simulation evidence available
- Can get artefacts in fitted function
  - Problems with over-interpretation
  - May not be transportable to other datasets (validation)
- Highly correlated terms
  - Need to orthogonalise

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**A difficult issue: model selection**

- Scale of model
  - Hazard, odds, probit, etc.
- Baseline (spline terms)
  - Done separate or simultaneously with covariates?
- How to do scale, variable and function selection?
  - E.g. when have prognostic factors in cancer
- Many possible covariate x time interactions give serious multiplicity problem
  - Forward selection?
- Assessing model stability (e.g. bootstrap)

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### Paul Lambert

- Cure models – mixture and non-mixture formulations
- Seems particularly appropriate approach in relative survival context
  - In most primary cancers, some patients will be cured
  - For metastatic (e.g. stage 4) cancer, cure proportion is nearly 0
- Preference for non-mixture model
  - More realistic
  - Is also interpretable as a mixture model

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### Issues

- Are the models identifiable?
  - Model with excess hazards converging towards zero may fit equally well – and could use more flexible distributional specification
- Robustness - estimate of cure fraction ( $\pi$ ) depends on choice of parametric survival distribution
- Is it possible to fit Royston-Parmar-Nelson distributions to  $S(t)$ ?
- How to choose a model – many possibilities?

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### Ula Nur

- Handle missing covariate values by multiple imputation (MI)
- Create  $m$  complete datasets (e.g.  $m = 10$ )
- Requires a (complex) imputation model
  - To make MAR assumption more plausible
- Do MI using `ice`
- Combine results from models fit by `strs`, `strel` etc using `micombine` or `mim`
  - `mim` is preferred command now

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### Issues

- Handling of categorical covariates needs care
  - Use `passive()` and `substitute()` options in `ice`
- Not clear how/whether survival time should be transformed in `ice` model
  - General issue in survival analysis with missing data
  - Probably depends on substantive model to be fitted
- Since covariate x time interactions are a feature of RS models, should consider including them in `ice` model
  - Omission will cause bias towards zero

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### Future

- What are the main aims of relative survival models?
- If *description* then *goodness of fit* and *interpretability* are important
- If *prediction* in independent data then *external validation* is important
- What implications would these aims have for the preferred method of modelling?
- E.g. (when) should cure models be the approach of choice?

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### Further applications

- Meta analysis of relative survival functions across hospitals, regions, countries, etc?
- Role in regular prognostic modelling?
- Role in economic evaluation of cancer therapies using data from clinical trials?
  - Estimate disease-related years of life lost

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### Stata

- Standardise popmort file specification for use by strel, strsm\* and other applications?
- Recommendation of particular approaches/Stata commands to answer specific questions?