An introduction to flexible parametric survival models

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- About me.
- A 'non-technical' introduction to flexible parametric survival models and why I like them.
- Implementation in Stata (time permitting).
- Regression standardisation. (time permitting).

- Born in Sydney Australia; studied mathematics and statistics in Newcastle (Australia).
- Worked in health services research; dabbled in industrial process control and quality improvement.
- Arrived in Sweden November 1993 for a 10 month visit to cancer epidemiology unit at KI. Stayed in Sweden for most of my PhD.
- Short Postdoc periods at Finnish Cancer Registry and Karolinska Institutet (cancer epidemiology).
- Joined MEB (MEP) in March 1999, attracted by the strong research environment and possibilities in register-based epidemiology.

- Development and application of methods for population-based cancer survival analysis, particularly the estimation and modeling of relative/net survival.
- General interest in statistical aspects of the design, analysis, and reporting of epidemiological studies.
- Epidemiology, with particular focus on cancer epidemiology.
- Lots of administrative work (deputy head of deptartment and head of biostatistics group).
- Programme director for master's programme in biostatistics and data science (commences HT2024).

• Commonly used models have the same basic formulation.

 $h_i(t) = h_0(t) \exp(\mathbf{x}_i \beta)$ $\ln(h_i(t)) = \ln(h_0(t)) + \mathbf{x}_i \beta$

- Proportional hazards assumed by default (but can be relaxed).
- Primary difference is in specification of the baseline hazard:
 - Cox model: $h_0(t)$ an arbitrary function of time; not estimated.
 - Poisson regression model: $h_0(t)$ is a step function.
 - Weibull model: $h_0(t) = \lambda \gamma t^{\gamma-1}$
 - Flexible parametric model: $h_0(t)$ modelled using splines.

Why I use flexible parametric survival models

- I analyse large population-based datasets where
 - The proportional hazards assumption is rarely appropriate.
 - The hazard function is of interest.
 - A hazard ratio does not tell the whole story.
- I model excess mortality/net survival among cancer patients.
 - Not possible to fit the Cox model.
 - Proportional excess hazards assumption is rarely appropriate.
 - Quantities other than the excess hazard ratio are of interest.
- Quantification and presentation of absolute risks and rates.
 - Should be done more than it is.
 - Much easier with parametric estimate of the baseline hazard.
- Many useful extensions are much easier in a parametric setting.

European Journal of Cancer 95 (2018) 52-58



Original Research

Bladder cancer survival: Women better off in the long run



Bettina Kulle Andreassen ^{a,*}, Tom Kristian Grimsrud ^a, Erik Skaaheim Haug ^{b,c}

• See Radkiewicz et al. (2017) [1] for a similar Swedish study.

Time-varying excess hazard ratio [2]



Fig. 2. Risk ratio (excess mortality rate ratio) including confidence intervals for men versus women with bladder cancer diagnosis. The

Baseline excess mortality rates [2]



Marginal and standardised survival [2, 3]



Fig. 3. Relative survival for men, women and women assuming the same T-stage distribution as men. Black (grey) lines: mean survival curve for men (women); Dashed grey line: survival curve for women when assuming men's covariate pattern.

Loss in expectation of life: CML (Sweden) [4]



Expectation of life



Expectation of life



Loss in expectation of life



Why use the loss in expectation of life?

- Survival statistics can be confusing! A change in the life expectancy can be understood by most people.
- Interpreted in years and measured over the entire lifespan.
- Can fit complex models and still get a simple interpretation.
- Can be useful for individuals to understand the impact of a diagnosis of cancer on their life expectancy.
- Can quantify the cancer burden in society. Not subject to the challenges one faces in defining and interpreting 'avoidable premature deaths'.
- Is a key input in health technology assessment and cost-effectiveness studies.

- I use and advocate flexible parametric survival models. However,
- There is nothing wrong with using a Cox model.
- If you only want to estimate a hazard ratio and you 'know' you have proportional hazards then a Cox model is ideal.
- Can relax the PH assumption in the Cox model, and can estimate quantities other than HR.
- However, a parametric approach makes it easier to estimate quantities that provide more insight and may be more relevant to your research question.
- You will get the same hazard ratio, but a whole lot more.

An interview with Sir David Cox (Reid 1994 [5])

- Reid "What do you think of the cottage industry that's grown up around [the Cox model]?"
- Cox "In the light of further results one knows since, I think I would normally want to tackle the problem parametrically. ... I'm not keen on non-parametric formulations normally."
- Reid "So if you had a set of censored survival data today, you might rather fit a parametric model, even though there was a feeling among the medical statisticians that that wasn't quite right."
- Cox "That's right, but since then various people have shown that the answers are very insensitive to the parametric formulation of the underlying distribution. And if you want to do things like predict the outcome for a particular patient, it's much more convenient to do that parametrically."

Example: survival of patients diagnosed with colon carcinoma

- I will use this dataset throughout the lecture.
- Patients diagnosed with colon carcinoma 1984–95. Potential follow-up to end of 1995; censored after 10 years.
- Outcome is death due to colon carcinoma.
- Interest is in the effect of clinical stage at diagnosis (distant metastases vs no distant metastases).
- How might we specify a statistical model for these data?



Smoothed empirical hazards (cancer-specific mortality rates) sts graph, by(distant) hazard kernel(epan2)



The Cox proportional hazards model

- The 'intercept' in the Cox model [6], the hazard (event rate) for individuals with all covariates x at the reference level, can be thought of as an arbitrary function of time¹, often called the baseline hazard and denoted by h₀(t).
- The hazard at time *t* for individual with other covariate values is a multiple of the baseline

$$h(t|x) = h_0(t) \exp(x\beta).$$

Alternatively

$$\ln[h(t|x)] = \ln[h_0(t)] + x\beta.$$

 Does not explicitly estimate h₀(t) while estimating the log hazard ratios (β).

¹time t can be defined in many ways, e.g., attained age, time-on-study, calendar time, etc.

Fit a Cox model to estimate the mortality rate ratio

stcox distant	
failure _d:	status == 1
analysis time _t:	(exit-origin)/365.25
origin:	time dx
note:	time>10 trimmed

Cox regression -- Breslow method for ties



Fitted hazards from parametric survival model (exponential) 1.6 Hazard Ratios Not distant Cox: 6.64 Distant Exponential: 10.04 N Hazard .8 4 Hazard ratio: 10.04 0 2 т 6 Ŕ 10 Δ 0

Years since diagnosis



We can make Poisson regression more similar, and even equivalent to, Cox regression

- We can make Poisson regression more similar to Cox regression by using a larger number of smaller intervals.
- If we split at each event time, then the estimates from Poisson regression are equivalent to those from Cox regression.

www.pauldickman.com/software/stata/compare-cox-poisson/

Fitted hazards from parametric survival model (Weibull) 1.6 Hazard Ratios Cox: 6.64 Exponential: 10.04 Weibull: 7.41 1.2 Hazard Not distant ထ Distant 4 Hazard ratio: 7.41

0 -						
	0	2	4 Years since diad	6 anosis	8	10
				gilloolo		



Fitted cumulative hazards from Weibull model





Fitted hazards from flexible parametric model (5df)



Flexible Parametric Survival Models [7, 10, 11]

- First introduced by Royston and Parmar (2002) [7].
- Parametric estimate of the baseline hazard without the usual restrictions on the shape (i.e., flexible).
- Applicable for 'standard' and relative survival models.
- Can fit relative survival cure models (Andersson 2011) [8].
- Once we have a parametric expression for the baseline hazard we derive other quantities of interest (e.g., survival, hazard ratio, hazard differences, expectation of life).
- Can be fitted in Stata (stpm2) and R (rstpm2 or flexsurv).
- Can also be estimated on the log-hazard scale [9]

$$h_i(t|\mathbf{x}_i,\beta) = h_0(t) \exp{(\mathbf{x}_i\beta)}$$

- Advantage: The baseline hazard, $h_0(t)$ is not directly estimated from a Cox model.
- Disadvantage: The baseline hazard, $h_0(t)$ is not directly estimated from a Cox model.

Flexible Parametric Models: Basic Idea

• Consider a Weibull survival curve.

$$S(t) = \exp\left(-\lambda t^{\gamma}
ight)$$

• If we transform to the log cumulative hazard scale.

$$\ln [H(t)] = \ln[-\ln(S(t))]$$
$$\ln [H(t)] = \ln(\lambda) + \gamma \ln(t)$$

• The log cumulative hazard is a linear function of ln(t)

Introducing covariates gives

$$\ln \left[H(t|\mathbf{x}_i)\right] = \ln(\lambda) + \gamma \ln(t) + \mathbf{x}_i \boldsymbol{\beta}$$

• Rather than assuming linearity with ln(t) flexible parametric models use restricted cubic splines for ln(t).

Fitted cumulative hazards from Weibull model




Flexible parametric models: Incorporating splines

• We model on the log cumulative hazard scale.

 $\ln[H(t|\mathbf{x}_i)] = \ln[H_0(t)] + \mathbf{x}_i \boldsymbol{\beta}$

- This is a proportional hazards model.
- Restricted cubic splines are used to model the log baseline cumulative hazard.
- For example, with 4 knots we can write

$$\ln [H(t|\mathbf{x}_i)] = \eta_i = \underbrace{\gamma_0 + \gamma_1 z_{1i} + \gamma_2 z_{2i} + \gamma_3 z_{3i}}_{\text{log baseline}} + \underbrace{\mathbf{x}_i \boldsymbol{\beta}}_{\text{log hazard}}$$



Course in Italy, 5–10 June 2023, http://cansurv.net/ Dickman, Lambert, Rutherford, Andersson, Syriopoulou

Sensitivity to choice of knots; Simulation study by Rutherford et al. (2013) [12]

- 'Through the use of simulation we show that, provided a sufficient number of knots are used, the approximated hazard functions given by restricted cubic splines fit closely to the true function for a range of complex hazard shapes.'
- 'The simulation results also highlight the insensitivity of the estimated relative effects (hazard ratios) to the correct specification of the baseline hazard.'

Sensitivity analysis by Syriopoulou et al. (2019) [13]

- 'Although estimates do not depend heavily on the number of knots, too few knots should be avoided, as they can result in a poor fit.'
- 'Interactive graphs engage researchers in assessing model sensitivity to a wide range of scenarios and their use is highly encouraged.'

Implementation in Stata [10]

stpm2 available from SSC

ssc install stpm2

All-cause or cause-specific survival

stpm2 distant, scale(hazard) df(5)

Relative survival (excess mortality)

stpm2 distant, scale(hazard) df(5) bhazard(rate)

Time-dependent effects

stpm2 distant, sc(hazard) df(5) bh(rate) tvc(distant) dftvc(3)

Cure model

stpm2 distant, sc(hazard) df(5) bh(rate) tvc(distant) dftvc(3) cure

Continuing with the colon carcinoma example

- Patients diagnosed with colon carcinoma 1984–95. Potential follow-up to end of 1995; censored after 10 years.
- Outcome is death due to colon carcinoma.
- We have restricted to patients with localised stage.
- This example will be used for the remainder of the lecture.

Fitting proportional hazards models

• I will start with PH models to illustrate basic concepts and will show later how to relax the PH assumption.

Proportional hazards models

. stcox male agegrp2 agegrp3 agegrp4
. stpm2 male agegrp2 agegrp3 agegrp4, scale(hazard) df(5)

- The scale(hazard) option requests the model be fitted on the log cumulative hazard scale.
- The df(5) option implies using 4 internal knots and 2 boundary knots for the baseline cumulative hazard.

Cox proportional hazards model

. stcox male agegrp2 agegrp3 agegrp4						
Cox regression with Breslow method for ties						
No. of subjects = 6,274 Number of obs = 6,274 No. of failures = 1,687 Time at risk = 30.962.0616						
			LR	chi2(4) =	155.93	
Log likelihood = -1407	3.066		Pro	b > chi2 =	0.0000	
_t Haz. ratio	Std. err.	z	P> z	[95% conf.	interval]	
male 1.098541	.0548618	1.88	0.060	.9961089	1.211507	
agegrp2 .9006346	.1257767	-0.75	0.454	.6849762	1.184191	
agegrp3 1.216113	.1539427	1.55	0.122	.9489076	1.558562	
agegrp4 2.030934	.2567928	5.60	0.000	1.585146	2.602091	

• The above estimates are adjusted for the baseline hazard (i.e., that mortality may depend on time since diagnosis) but the baseline hazard is not estimated along with the other parameters.

Flexible parametric proportional hazards model

. stpm2 male agegrp2 agegrp3 agegrp4, scale(hazard) df(5) eform

Log likelihood = -5898.9448

Number of obs = 6,274

xb male 1.101218 .054999 agegrp2 .9029138 .126094 agegrp3 1.223325 .154860 agegrp4 2.059039 .260378				
_rcs1 2.324953 .045463 _rcs2 1.052631 .014262 _rcs3 1.010869 .007523 _rcs4 1.081719 .007031 _rcs5 1.004954 .004649 _cons .1460823 .018125	399 1.93 349 -0.73 501 1.59 789 5.71 533 43.15 523 3.79 236 1.45 315 12.08 494 1.07 255 -15.50	0.054 0.465 0.111 0.000 0.000 0.000 0.146 0.000 0.285 0.000	.998528 .6867097 .9545278 1.607032 2.237532 1.025045 .9962299 1.068025 .9958821 .1145467	1.214468 1.187188 1.567816 2.638181 2.415789 1.080959 1.025723 1.095589 1.014108 .1862998

- The eform option requests exponentiated parameter estimates (i.e., hazard ratios).
- The _rcs parameters are the spline basis vectors; the estimates do not have a simple interpretation.

Comparison of estimates, PH models

Variable	cox	stpm2		
male	1.0985 0.0549	1.1012 0.0550		
agegrp2	0.9006 0.1258	0.9029 0.1261		
agegrp3 	1.2161 0.1539	1.2233 0.1549		
agegrp4 	2.0309 0.2568	$2.0590 \\ 0.2604$		
Legend: HR/se				

- The hazard ratios and standard errors are similar.
- I have yet to find an example of a proportional hazards model where there is a large difference in the estimated hazard ratios.

• stpm2 has a very powerful postestimation command, predict, for model-based predictions.

Predicting the survival and hazard functions

- . predict survpred, survival
- predict hazpred, hazard
 - For confidence intervals, include the ci option.
 - Model-based prediction is very powerful, but should be performed with caution.
 - Following is a plot of survpred (predicted cause-specific survival) against time (_t) for the model we just fitted.

Predicted survival, but probably not as we had hoped twoway (line survpred _t, sort)



Survival predictions in Stata - technical details

- For each observation, Stata predicts the requested quantities at the value of _t (exit time).
- For each value of _t there are 8 possible predicted values of the survival function (one for each combination of age and sex).
- Use the at() option to predict for a specified covariate pattern.

Predicted survival for males and females in age group 2

. predict s_m_age2, survival at(male 1 agegrp2 1) zeros . predict s_f_age2, survival at(male 0 agegrp2 1) zeros

• The zeros option sets all covariates not in at() to zero.

Predicted survival by sex, ages 60-74, from PH model twoway (line s_m_age2 _t, sort) (line s_f_age2 _t, sort)



Survival predictions from PH model

- Predictions on the previous slide are based on a PH model, which may or may not be appropriate.
- On the next slide we will see how to relax the PH assumption.
- These are conditional (rather than marginal) estimates. That is, estimates of survival for an individual with specified values of sex and age group.
- I will show later how to obtain marginal (population-averaged) estimates.

Time-dependent effects (non-proportional hazards)

• Fitting time-dependent effects is done using the tvc() and dftvc() options.

stpm2 with non-PH

Cox model with non-PH

stcox male agegrp2-agegrp4, tvc(male agegrp2-agegrp4) texp(_t)

• We are considering time-varying *coefficients*, not time-varying *covariates*.

• Syntax for predict is same as with PH model, but we now have the option of estimating time-varying hazard ratios using the hrnumerator() and hrdenominator() options.

predict s_m_age2_nonph, survival at(male 1 agegrp2 1) zeros
predict s_f_age2_nonph, survival at(male 0 agegrp2 1) zeros
// predict time-varying excess hazard ratio (males/females)
predict hr sex. hrnumerator(male 1) hrdenominator(male 0) ci

Predicted hazards (non-PH model)



Predicted hazard ratio for males/females



Time-varying excess hazard ratio [2]



Fig. 2. Risk ratio (excess mortality rate ratio) including confidence intervals for men versus women with bladder cancer diagnosis. The

The predict command is extremely powerful!

Syntax of predict and how to access the help file

- . predict newvar [if] [in] [, statistic]
- help stpm2 postestimation
 - Statistics for predict include:
 - sdiff difference in survival functions hdiff difference in hazard functions rmst restricted mean survival time lifelost loss in expectation of life (after a relative survival model) cure cure proportion (after fitting a cure model) uncured survival function for uncured (after fitting a cure model) meansurv population averaged (marginal) survival

Marginal (population-averaged) survival curves: average of individual predictions

• The predicted survival function for individual *i* is

$$\widehat{S}_i(t) = \exp\left(-H_0(t)\exp\left(\mathbf{x}_i\beta\right)\right)$$

• We average over all predicted survival functions

$$\widehat{S}^{P}(t) = rac{1}{N}\sum_{i=1}^{N}\widehat{S}_{i}(t)$$

- The model can be as complex as required (continuous covariates, interactions, non-linear functions, non-proportional hazards).
- We are predicting a function, not S(t) at a single time point.

Software for marginal measures and regression standardisation

- With Stata stpm2, the meansurv option to predict produces an average of predicted survival curves for each observation.
- standsurv is much faster and has more features, see: https://pclambert.net/software/standsurv/.
- R users can use the stdReg package (Arvid Sjölander).

Marginal survival curves with stpm2, predict meansurv

- s_marginal is the average of all 6,274 predicted curves.
- s_m_marginal is the average of the 2,620 curves for males.
- s_f_marginal is the average of all 3,654 curves for females.
- s_m_marginal and s_f_marginal are not comparable, but we have estimates for the entire population (i.e., not conditional).

The Hazards of Hazard Ratios

Miguel A. Hernán

The hazard ratio (HR) is the main, and often the only, effect measure reported in many epidemiologic studies. For dichotomous, non-time-varying exposures, the HR is defined as the hazard in the exposed groups divided by the hazard in the unexposed groups. For all practical purposes, hazards can be thought of as incidence rates and thus the HR can be roughly interpreted as the incidence rate ratio. The HR is commonly and conveniently estimated via a Cox proportional hazards model, which can include potential confounders as covariates.

Unfortunately, the use of the HR for causal inference is not straightforward even in the absence of unmeasured confounding, measurement error, and model misspecification. Endowing a HR with a causal interpretation is risky for 2 key reasons: the HR may change over time, and the HR has a built-in selection bias. Here I review these 2 problems and

Standardised survival curves

 Marginal (population-averaged) survival curves, but 'comparable' (standardised).

```
// Standardised survival (using entire cohort as standard)
predict s_m_std, at(male 1) meansurv timevar(temptime)
predict s_f_std, at(male 0) meansurv timevar(temptime)
// Standardised survival (using males as the standard)
predict s_m_std_m if male==1, at(male 1) meansurv timevar(temptime)
predict s_f_std_m if male==1, at(male 0) meansurv timevar(temptime)
```

- If the model is appropriate and there are no unmeasured confounders, the difference in standardised survival probabilities is an estimate of the causal effect of treatment on survival.
- Under assumptions, the difference between the bottom two estimates is the causal effect among the exposed (if being male is the exposure).

Marginal and standardised survival [2, 3]



Fig. 3. Relative survival for men, women and women assuming the same T-stage distribution as men. Black (grey) lines: mean survival curve for men (women); Dashed grey line: survival curve for women when assuming men's covariate pattern.

Standardised survival curves (with some math)

- When interest lies in comparing the survival of (two) exposure groups we can standardize to the same covariate distribution.
- Let X be the exposure of interest (e.g., male sex).
- Let Z denote the set of measured covariates (age group).

$$\widehat{R}^{P}(t|X=x,Z) = rac{1}{N}\sum_{i=1}^{N}\widehat{R}_{i}(t|X=x,Z=z_{i})$$

- Note that the average is over the marginal distribution of Z, not over the conditional distribution of Z among those with X = x.
- We are forcing the same covariate distribution on both exposure groups.

Standardised survival curves

• We first predict a relative survival curve for all 6,274 patients under the assumption they are male, and average these curves.

$$\widehat{\mathcal{R}}^{\mathcal{P}}(t|X=\textit{male},Z) = rac{1}{N}\sum_{i=1}^{N}\widehat{\mathcal{R}}_{i}\left(t|X=\textit{male},Z=z_{i}
ight)$$

• We then predict a relative survival curve for all 6,274 patients under the assumption they are female, and average these curves.

$$\widehat{R}^{P}(t|X = \textit{female}, Z) = \frac{1}{N} \sum_{i=1}^{N} \widehat{R}_{i}(t|X = \textit{female}, Z = z_{i})$$

 Both resulting marginal relative survival curves are averaged over the same covariate distribution (age distribution in the entire population). The two curves have been age-standardised and are comparable (with respect to confounding by age).

- 252 patients entering a renal dialysis program in Leicestershire, England 1982-1991 with follow-up to the end of 1994.
- Interest in difference in survival by ethnicity (Non-South Asian vs South Asian).
- At the time of the study, approximately 25% of the population were of South Asian origin.

Kaplan-Meier Curves - Renal Replacement Therapy



The meansurv option

```
stpm2 asian age, df(3) scale(hazard)
/* Age distribution for study population as a whole */
predict meansurv_pop0, meansurv at(asian 0)
predict meansurv_pop1, meansurv at(asian 1)
/* Age distribution for non-asians */
predict meansurv_pop1b if asian == 0, meansurv at(asian 0)
predict meansurv_pop1b if asian == 0, meansurv at(asian 1)
/* Age distribution for asians */
```

```
predict meansurv_popOc if asian == 1, meansurv at(asian 0)
predict meansurv_pop1c if asian == 1, meansurv at(asian 1)
```

 S(t) calculated for each subject in the study population and averaged.

Standardized Survival Curve 1



Standardized Survival Curve 2



Standardized Survival Curve 3



Standardised survival probabilities: a useful and informative tool for reporting regression models for survival data

Elisavet Syriopoulou [[]^{1⊠}, Tove Wästerlid^{2,3}, Paul C. Lambert^{1,4} and Therese M.-L. Andersson [[]

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BACKGROUND: When interested in studying the effect of a treatment (or other exposure) on a time-to-event outcome, the most popular approach is to estimate survival probabilities using the Kaplan–Meier estimator. In the presence of confounding, regression models are fitted, and results are often summarised as hazard ratios. However, despite their broad use, hazard ratios are frequently misinterpreted as relative risks instead of relative rates.

METHODS: We discuss measures for summarising the analysis from a regression model that overcome some of the limitations associated with hazard ratios. Such measures are the standardised survival probabilities for treated and untreated: survival probabilities if everyone in the population received treatment and if everyone did not. The difference between treatment arms can be calculated to provide a measure for the treatment effect.

RESULTS: Using publicly available data on breast cancer, we demonstrated the usefulness of standardised survival probabilities for comparing the experience between treated and untreated after adjusting for confounding. We also showed that additional important research questions can be addressed by standardising among subgroups of the total population.

DISCUSSION: Standardised survival probabilities are a useful way to report the treatment effect while adjusting for confounding and have an informative interpretation in terms of risk.

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Original article

Marginal measures and causal effects using the relative survival framework

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- Cure models [8].
- Random effect models [16].
- Joint models [17].
- Multi-state models
- Competing Risks
 - Cause-specific models [18]
 - Direct modelling (subhazards) [19, 19].
- Restricted mean survival time [20].
- Prognostic modelling.

- There is nothing wrong with using a Cox model.
- If you only want to estimate a hazard ratio and that you 'know' you have proportional hazards then a Cox model is ideal.
- Can relax the PH assumption in the Cox model, and can estimate quantities other than HR.
- However, a parametric approach makes it easier to estimate quantities that provide more insight and may be more relevant to your research question.
- You will get the same hazard ratio, but a whole lot more.

Annals of Internal Medicine

ORIGINAL RESEARCH

Risk for Arterial and Venous Thrombosis in Patients With Myeloproliferative Neoplasms A Population-Based Cohort Study

Malin Hultcrantz, MD, PhD; Magnus Björkholm, MD, PhD; Paul W. Dickman, MSc, PhD; Ola Landgren, MD, PhD; Åsa R. Derolf, MD, PhD; Sigurdur Y. Kristinsson, MD, PhD*; and Therese M.L. Andersson, MSc, PhD*

Background: Patients with myeloproliferative neoplasms (MPNs) are reported to be at increased risk for thrombotic events. However, no population-based study has estimated this excess risk compared with matched control participants.

Objective: To assess risk for arterial and venous thrombosis in patients with MPNs compared with matched control participants.

Design: Matched cohort study.

Setting: Population-based setting in Sweden from 1987 to 2009, with follow-up to 2010.

Patients: 9429 patients with MPNs and 35 820 matched control participants.

Measurements: The primary outcomes were rates of arterial and venous thrombosis. Flexible parametric models were used to calculate hazard ratios (HRs) and cumulative incidence with 95% Cls.

Results: The HRs for arterial thrombosis among patients with MPNs compared with control participants at 3 months, 1 year, and 5 years were 3.0 (95% Cl, 2.7 to 3.4), 2.0 (Cl, 1.8 to 2.2), and 1.5 (Cl, 1.4 to 1.6), respectively. The corresponding HRs for venous thrombosis were 9.7 (Cl, 7.8 to 12.0), 4.7 (Cl, 4.0 to 5.4), and 3.2 (Cl, 2.9 to 3.6). The rate was significantly elevated across all age groups and was similar among MPN subtypes. The 5-year cumulative incidence of thrombosis in patients with MPNs showed an initial rapid increase followed by gentler increases during follow-up. The HR for venous thrombosis decreased during more recent calendar periods.

Limitation: No information on individual laboratory results or treatment.

Conclusion: Patients with MPNs across all age groups have a significantly increased rate of arterial and venous thrombosis compared with matched control participants, with the highest rates at and shortly after diagnosis. Decreases in the rate of venous thrombosis over time likely reflect advances in clinical management.

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* Drs. Kristinsson and Andersson contributed equally to this work.

Figure 1. Arterial (*top*) and venous (*bottom*) thrombosis during follow-up in patients with MPNs versus matched control participants.



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